

1 *Improvements in Thermal Efficiency and Exhaust Emissions with Ozone*  
2 *addition in a Natural Gas-Diesel Dual Fuel Engine*

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9  
10 **Abstract**

11 Here, ozone (O<sub>3</sub>) was introduced into the intake air in a natural gas fueled engine ignited  
12 by diesel fuel, a natural gas – diesel dual fuel engine, to utilize the reactive O-radicals  
13 decomposed from the O<sub>3</sub> for the promotion of the ignition and for improvements in the  
14 thermal efficiency and exhaust emissions. The engine experiments were performed over  
15 a range of equivalence ratios of the natural gas in a single cylinder engine. The timing of  
16 the pilot injection of the diesel fuel was varied from early in the compression stroke to  
17 near top dead center to examine the changes in the effects of the O<sub>3</sub> addition on the  
18 ignition and combustion with the pilot injection timing while varying the O<sub>3</sub> concentration.  
19 The results showed that the combination of the O<sub>3</sub> addition and the early pilot injection is  
20 a means to improve the thermal efficiency and unburned emissions with a small amount

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21 of O<sub>3</sub>. Further, the improvement in the thermal efficiency and the reduction of the  
22 unburned hydrocarbons with the O<sub>3</sub> addition are more pronounced for lower equivalence  
23 ratios of natural gas, while the O<sub>3</sub> addition has a limited effect on the thermal efficiency  
24 and the unburned hydrocarbons for higher equivalence ratios of the natural gas.

25

26 **Keywords:** Dual Fuel Engine, Ozone, Natural Gas, Diesel fuel, Pilot injection, Thermal  
27 Efficiency, Exhaust Emissions

28

29 **Nomenclature:**

30	CA50	Mass burned at 50% crank angle [°CA ATDC]
31	$(dp/d\theta)_{\max}$	Maximum rate of pressure rise [MPa/°CA]
32	$Q_{\text{burn}}$	Energy released with chemical reactions [J]
33	$Q_{\text{cool}}$	Energy lost due to cooling [J]
34	$Q_{\text{fuel}}$	Total fuel energy supplied [J]
35	$V_c$	Clearance volume at the top dead center [m <sup>3</sup> ]
36	$V_h$	Displacement volume [m <sup>3</sup> ]
37	$V_\theta$	Volume of combustion chamber at crank angle $\theta$

38

39 **Greek symbols:**

40	$\varphi_{\text{cool}}$	Cooling loss [%]
41	$\varphi_{\text{gas}}$	Equivalence ratio of natural gas [-]
42	$\theta$	Crank angle [°CA]
43	$\theta_{\text{pilot}}$	Pilot injection timing of diesel fuel [°CA ATDC]
44	$\eta_i$	Indicated thermal efficiency [%]
45	$\eta_{\text{glh}}$	Degree of constant volume heat release [%]
46	$\eta_{\text{comb}}$	Combustion efficiency [%]
47	$\eta_u$	Unburned loss [%]

48 **1. Introduction**

49 Natural gas fueled engines ignited by diesel fuel, natural gas – diesel dual fuel engines  
50 in the following, can help to reduce the environmental effect of internal combustion  
51 engines, as it may provide higher thermal efficiency with lower exhaust emissions, and  
52 the methane, which is the primary constituent of natural gas, should be a candidate among  
53 carbon neutral fuels as it can be generated through carbon dioxide (CO<sub>2</sub>)-free hydrogen  
54 derived from renewable energy sources and the CO<sub>2</sub> emitted from processes such as  
55 biomass power generation.

56 The drawback of such engines is that the unburned methane emissions which are  
57 released into the atmosphere have a warming potential many times that of carbon dioxide.  
58 The previous research reduced unburned methane emissions with optimization of the  
59 injection strategy of the diesel fuel and combustion chamber geometry, and by intake gas  
60 throttling [1-5]. Further improvements, however, would be needed as lean burn operation  
61 with supercharging, which are expected to be an effective means to increase thermal  
62 efficiency, may cause increases in the unburned methane emissions.

63 Another possible way to address the problem of increased methane release could be  
64 the addition of ozone (O<sub>3</sub>) to the intake air of engines. The O<sub>3</sub> addition is promising in  
65 terms of rapid response and low energy consumption as O<sub>3</sub> can be produced with non-

66 equilibrium plasma. The decomposition of  $O_3$  to O-radicals occurs at temperatures around  
67 500 K to 600 K [6-9]. Together with the  $O_3$  decomposition, a recombination reaction of  
68 the O-radicals is initiated to reduce them to oxygen molecules ( $O_2$ ), while the O-radicals  
69 react with hydrocarbons when there are coexisting hydrocarbons, enhancing the oxidation  
70 reaction [9-11].

71 The  $O_3$  addition has been utilized to control the ignition timing in homogeneous  
72 charge compression ignition (HCCI) engines where hydrocarbons are premixed in the  
73 cylinder and the ignition of the hydrocarbons is enhanced by the reaction with the O-  
74 radicals produced via the ozone decomposition [12-15]. The ignition enhancement effects  
75 due to the  $O_3$  addition have also been utilized in gasoline compression ignition (GCI)  
76 engines employing a two-stage direct injection strategy, in which the first injection is  
77 implemented before the  $O_3$  decomposition to make the first injected fuel react with the  
78 O-radicals, and the ignition delay of the second injection is controlled by the temperature  
79 increase and the chemical species generated due to the first fuel injection [9, 16-17].

80 Nishida et al. [18] introduced  $O_3$  into the intake air together with natural gas and  
81 injected diesel fuel directly into the cylinder near top dead center. That report showed that  
82 an  $O_3$  concentration of 1000 ppm or more was needed to enhance the ignition [18]. This  
83  $O_3$  concentration is considerably higher than that used to enhance the combustion of

84 premixed gasoline components, that is less than 100 ppm [10, 11, 15-17], and  
85 considerable energy amounts are consumed to generate the O<sub>3</sub> concentration above 1000  
86 ppm [19]. The differences in the required O<sub>3</sub> concentration between the gasoline  
87 components and the natural gas would suggest that the oxidation reactions of larger  
88 hydrocarbons are more likely to be affected by the O-radicals.

89 The purpose of the present study is to develop a means to improve the thermal  
90 efficiency and exhaust emissions of natural gas-diesel dual fuel engines by utilizing the  
91 ignition enhancement effects of the O<sub>3</sub>. To achieve this, an experimental study was carried  
92 out with a single cylinder engine. To examine the effects of the O<sub>3</sub> addition on the ignition  
93 of diesel fuel which consists of larger hydrocarbons, the pilot injection timing of the diesel  
94 fuel was varied from the early in the compression stroke to top dead center while varying  
95 the seeded O<sub>3</sub> concentration. Further, the engine performance and exhaust emissions were  
96 examined over a range of engine loads to elucidate the changes in the requirement of the  
97 O<sub>3</sub> concentration with the equivalence ratio of the natural gas.

## 98 **2. Experimental Setup**

99 The specifications of the test engine are detailed in Table 1. The test engine was a  
100 single cylinder engine equipped with a common-rail fuel injection system. A

101 commercially available injector (DENSO, G4S) having an 8-hole nozzle with the nominal  
102 hole diameter of 0.125 mm and with the umbrella angle of 155° mounted on the cylinder  
103 head. The bore and stroke are 98 mm and 110 mm, and the displacement volume is 830  
104 cm<sup>3</sup>, the compression ratio is 17.6. A graphic of the piston is shown in Fig.1. The piston  
105 has a toroidal-shaped cavity which has a diameter of 62.1 mm. The engine was connected  
106 to an eddy current electric dynamometer (Tokyo Koki, W-130) to absorb the engine output.  
107 The test engine has a low pressure EGR pathway and a roots type blower (OGURA  
108 CLUTCH, TX04) for supercharging, but all the experiments were performed with  
109 naturally aspirated engine operations here.

110 An illustration of the experimental setup is shown in Fig.2. The piezoelectric pressure  
111 sensor (KISTLER, 6125B) was installed in the cylinder head, and the electric charge was  
112 converted into a voltage signal with a charge amplifier (KISTLER, 5011B). The voltage  
113 signal proportional to the in-cylinder pressure was recorded with a transient memory  
114 board at a resolution of 0.2° CA for 150 cycles. It may be possible to examine the effect  
115 of the ozone (O<sub>3</sub>) addition on the cycle-to-cycle variation with the data recorded for 150  
116 cycles. This is, however, outside the scope of the present study and will be examined in  
117 the future. In the present study, cycle-averaged profiles of pressure and rate of heat release  
118 are used to examine the combustion characteristics. Natural gas was delivered from a gas

119 cylinder into the intake pipe (diameter: 52.7 mm), located 450 mm upstream of the intake  
120 port with a mass flow controller (ALICAT, MCR-50SLPM-D). The composition of the  
121 natural gas could be varied from gas cylinder to gas cylinder, and the gas composition is  
122 detailed in Table 2, measured with a thermal conductivity detector (TCD) for one cylinder  
123 used as the reference in the present study.

124 Ozone ( $O_3$ ) was produced with an ozonizer (EcoDesign, ED-OG-S4AD) while  
125 introducing pure oxygen ( $O_2$ ) from a gas cylinder, and it was delivered into the intake  
126 pipe, 450 mm upstream of the intake port. It is possible to produce  $O_3$  from air as  
127 demonstrated in the previous study [9], but  $O_3$  was made from  $O_2$  to supply higher  
128 concentration of  $O_3$  to the engine in the present study. The  $O_2$  flow rate was measured  
129 with a rotameter embedded in the ozonizer. The  $O_3$  concentration was measured with a  
130 UV ozone monitor (EBARA, EG-600) before the ozone-containing oxygen was  
131 introduced into the intake pipe. The volume-based ozone concentration in the intake air  
132 was determined with the measured  $O_3$  concentration and the flow rates of the oxygen and  
133 the intake air which was measured using a differential pressure type flowmeter.

134 The concentrations of the total hydrocarbon (THC), carbon monoxide (CO), carbon  
135 dioxide ( $CO_2$ ), nitrogen oxides ( $NO_x$ ), and oxygen ( $O_2$ ) were measured at the intake and  
136 exhaust pipes with an exhaust gas analyzer (Best Sokki, BEX-5100D). The smoke

137 emissions were measured with a Bosch-type smoke meter (ZEXEL, DSM-20AN). As  
138 only insignificant smoke emissions were detected, no smoke data are presented in this  
139 paper.

### 140 **3. Experimental Results and Discussion**

#### 141 **3.1. Effects of the ozone addition on the combustion, engine performance, and** 142 **exhaust emissions at various pilot injection timings for a $\phi_{\text{gas}}$ of 0.42**

143 First, the effects of the pilot injection timing of the diesel fuel on the rate of heat  
144 release (ROHR) were investigated for the fixed equivalence ratio of the natural gas,  $\phi_{\text{gas}}$ ,  
145 of 0.42.

146 The experimental conditions are detailed in Table 3. The injection quantity of the  
147 diesel fuel was maintained constant at the heat value of the injected diesel fuel formed 11  
148 HV% of the total energy supplied. The pilot injection timing,  $\theta_{\text{pilot}}$ , was varied from -  
149 39°CA ATDC to 1°CA ATDC except where the maximum rate of pressure rise exceeded  
150 1.2 MPa/°CA and the rotation speed could not be maintained at 1200 rpm due to misfiring.  
151 The O<sub>3</sub> concentration was increased from 0 ppm to 560 ppm unless the indicated thermal  
152 efficiency begun to decrease with the increase of the O<sub>3</sub>. As the O<sub>2</sub> was supplied to  
153 generate the O<sub>3</sub>, the intake O<sub>2</sub> concentration was increased to 21.5 vol.%. No EGR and



154 no supercharging were employed in the experiments.

155 Figure 3 shows the changes in the profiles of the in-cylinder pressure and the ROHR  
156 with the pilot injection timing of the diesel fuel,  $\theta_{\text{pilot}}$ . The traces shown in Fig.3 (a) are  
157 for the late pilot injections, and those shown in (b) are for the early pilot injections. The  
158 number of the traces was reduced for simplicity, and the intermediate pilot injection  
159 timing,  $\theta_{\text{pilot}}$ , of  $-19^\circ\text{CA ATDC}$  was included in Fig.3 (a) and (b). Note that the combustion  
160 phase with the other pilot injection timings, not included in Fig.3, is in the order of the  
161 pilot injection timing.

162 At the late pilot injection timings,  $\theta_{\text{pilot}}$ , of  $1^\circ\text{CA ATDC}$ ,  $-4^\circ\text{CA ATDC}$ , and  $-9^\circ\text{CA}$   
163  $\text{ATDC}$ , two-stage combustion takes place: the first is a heat release by a mixture of the  
164 diesel fuel and natural gas, and the second is a heat release by the natural gas which is not  
165 mixed well with the diesel fuel. The advance of the pilot injection timing from  $1^\circ\text{CA}$   
166  $\text{ATDC}$  to  $-9^\circ\text{CA ATDC}$  advances the start of the first-stage combustion and increases the  
167 ROHR in the second-stage combustion. At the pilot injection timing,  $\theta_{\text{pilot}}$ , of  $-19^\circ\text{CA}$   
168  $\text{ATDC}$ , single-stage combustion occurs, followed by a lower ROHR due to the late  
169 combustion after  $10^\circ\text{CA ATDC}$ . This change in the ROHR pattern from  $\theta_{\text{pilot}} = -9^\circ\text{CA}$   
170  $\text{ATDC}$  to  $\theta_{\text{pilot}} = -19^\circ\text{CA ATDC}$  arises as the early pilot injection makes the diesel fuel  
171 become leaner and mixed well with the premixed natural gas. This type of combustion

172 can be seen in the reactivity controlled compression ignition (RCCI) strategy in which  
173 the early pilot injection of more reactive fuel is implemented directly into the cylinder  
174 where low reactive fuel is distributed [20-21]. Further advances of the pilot injection  
175 timing from  $-19^{\circ}\text{CA ATDC}$  cause retardations of the combustion phase as the diesel fuel  
176 mixture becomes much leaner, something that prolongs the ignition delay and combustion  
177 duration.

178 Second, the effects of the  $\text{O}_3$  addition were investigated for the fixed equivalence  
179 ratio of the natural gas,  $\phi_{\text{gas}}$ , of 0.42 while changing the  $\text{O}_3$  concentration and the pilot  
180 injection timing,  $\theta_{\text{pilot}}$ . Figure 4 shows the effects of the  $\text{O}_3$  concentration on the fuel mass  
181 burned at the 50% crank angle,  $\text{CA}_{50}$ . The addition of the 80 ppm  $\text{O}_3$  can prevent the  
182 misfiring caused by the early pilot injection. The  $\text{CA}_{50}$  advances with the increase of the  
183  $\text{O}_3$  concentration, and this is noticeable at pilot injection timings earlier than  $-19^{\circ}\text{CA}$   
184  $\text{ATDC}$ . At pilot injection timings later than  $-9^{\circ}\text{CA ATDC}$ , the  $\text{O}_3$  addition has a smaller  
185 influence on the  $\text{CA}_{50}$ , and the higher  $\text{O}_3$  concentration is needed to advance the  $\text{CA}_{50}$   
186 compared to the early pilot injection timings. This reason will be discussed in Fig.5.

187 Figure 5 shows the changes in the profiles of the in-cylinder pressure and the rate of  
188 heat release (ROHR) with the  $\text{O}_3$  concentration. Here, the two pilot injection timings,  $\theta_{\text{pilot}}$ ,  
189 of (a)  $-4^{\circ}\text{CA ATDC}$  and (b)  $-34^{\circ}\text{CA ATDC}$  were chosen as late and early injection timings.

190 The traces of all the O<sub>3</sub> concentrations are not shown in Fig.5 for simplicity, and it was  
191 confirmed that the combustion phase with the other O<sub>3</sub> concentrations, not included in  
192 Fig.5, was in the order of the O<sub>3</sub> concentration.

193 At the late  $\theta_{\text{pilot}}$  of -4°CA ATDC, the O<sub>3</sub> addition has a limited effect on the ROHR in  
194 the first-stage combustion, while the O<sub>3</sub> addition increases the ROHR in the second-stage  
195 combustion. This may be because the recombination reaction of the O-radicals which are  
196 produced by the decomposition of O<sub>3</sub> early in the compression stroke reduces O-radical  
197 concentration until late in the compression stroke [7, 9], and the O-radicals cannot  
198 enhance the first-stage combustion which is caused by the mixture of the diesel fuel and  
199 the natural gas. The premixed natural gas can react with the O-radicals, immediately after  
200 the O<sub>3</sub> decomposition, and the second-stage combustion which is mainly caused by the  
201 natural gas can be enhanced with O<sub>3</sub> of the order of hundreds of ppm.

202 At the early pilot injection timing,  $\theta_{\text{pilot}}$ , of -34°CA ATDC, the ignition of the single-  
203 stage combustion which strongly depends on chemical reactions of the diesel fuel is  
204 enhanced with the 50 ppm O<sub>3</sub>, and overall the combustion is advanced. This may be  
205 because the O<sub>3</sub> can remain undecomposed until the timing of diesel fuel injection, and the  
206 O-radicals produced from the O<sub>3</sub> would enhance the ignition of the diesel fuel which is  
207 mixed well with the premixed natural gas. A more detailed elucidation of the mechanism

208 of the detailed ignition processes is outside the scope of the present study, and the  
209 mechanism will be examined in future work.

210 Figure 6 compares the effects of the O<sub>3</sub> addition on the THC and NO<sub>x</sub> emissions  
211 between the  $\theta_{\text{pilot}}$  of -4°CA ATDC and -34°CA ATDC. Without the O<sub>3</sub> addition (0 ppm),  
212 the early pilot injection at -34°CA ATDC discharges the higher ratios of THC emissions  
213 than the late pilot injection at -4°CA ATDC. The O<sub>3</sub> addition reduces the THC emissions,  
214 and the reduction of the THC emissions becomes more remarkable with the early pilot  
215 injection. The primary reason of the reduction of the THC emissions may be the advanced  
216 combustion phase. The combustion phase is advanced with the O<sub>3</sub> addition for the early  
217 pilot injection at -34°CA ATDC as can be seen in Fig.5. At the late  $\theta_{\text{pilot}}$  of -4°CA ATDC,  
218 the O<sub>3</sub> addition increases the ROHR and decreases the duration in the second-stage  
219 combustion. As the cylinder pressure falls during the expansion stroke, the temperature  
220 of the unburned mixture decreases, and the unburned mixture remains unconsumed due  
221 to quenching of the oxidation process.

222 The nitrogen oxide (NO) formation rate depends on the flame temperature which is  
223 influenced by the local equivalence ratio in the combustion chamber. The NO formation  
224 rate changes with the combustion phase since the mixture which burns earlier in the cycle  
225 increases the peak cylinder pressure, and the higher peak cylinder pressures result in

226 higher flame temperatures and higher NO formation rates. Further the increased residence  
 227 time in high flame temperatures affects the amount of the NO formation. The late pilot  
 228 injection at -4°CA ATDC forms a locally rich mixture where NO<sub>x</sub> is generated. The NO<sub>x</sub>  
 229 emissions increase with the increase of the O<sub>3</sub> concentration due to the advanced  
 230 combustion phase. At the  $\theta_{\text{pilot}}$  of -34°CA ATDC, only low NO<sub>x</sub> emissions are discharged  
 231 due to the combustion of a leaner mixture of the diesel fuel, and the lower NO<sub>x</sub> emissions  
 232 are maintained when the O<sub>3</sub> concentration increases.

233 Figure 7 is a comparison of the effects of the ozone addition on the indicated thermal  
 234 efficiency,  $\eta_i$ , the degree of constant volume heat release,  $\eta_{\text{glh}}$ , the combustion efficiency,  
 235  $\eta_{\text{comb}}$ , and the ratio of cooling loss,  $\varphi_{\text{cool}}$ , at the late and early pilot injection timings. The  
 236 indicated thermal efficiency,  $\eta_i$ , is expressed by [22]

$$237 \quad \eta_i = \eta_{\text{th}} \eta_{\text{glh}} (1 - \eta_u - \varphi_{\text{cool}}) \quad (1)$$

238 Here,  $\eta_{\text{th}}$  is the theoretical thermal efficiency for the Otto Cycle. The unburned loss,  $\eta_u$ , is  
 239 defined as  $\eta_u = 1 - \eta_{\text{comb}}$ , and the combustion efficiency,  $\eta_{\text{comb}}$ , can be determined with the  
 240 measured exhaust emissions. The degree of constant volume heat release,  $\eta_{\text{glh}}$ , can be  
 241 calculated by the following equation with the consideration of the profile of the apparent  
 242 rate of heat release,  $dQ/d\theta$ :

$$243 \quad \eta_{\text{glh}} = \frac{1}{\eta_{\text{th}} \cdot Q} \int \left\{ 1 - \left( \frac{V_h + V_c}{V_\theta} \right)^{1-\kappa} \right\} \frac{dQ}{d\theta} d\theta \quad (2)$$

244 Here,  $\kappa$  is the ratio of specific heat,  $V_h$  is the displacement volume,  $V_c$  is the clearance  
245 volume at the top dead center, and  $V_\theta$  is the volume of the combustion chamber at crank  
246 angle  $\theta$ . The ratio of cooling loss,  $\varphi_{cool}$ , which is defined as  $\varphi_{cool} = Q_{cool}/Q_{fuel}$  where  
247  $Q_{cool}$  is the energy lost due to cooling, and  $Q_{fuel}$  is the total fuel energy supplied, can be  
248 calculated with Eq.(1) as the indicated thermal efficiency,  $\eta_i$ , and the unburned loss,  $\eta_u$ ,  
249 can be determined in the experiments. A similar approach for calculating the ratio of  
250 cooling loss,  $\varphi_{cool}$ , is proposed in a reference [23] in which the ratio of cooling loss is  
251 defined as  $\varphi_{cool} = Q_{cool}/Q_{burn}$  where  $Q_{burn}$  is the energy released by the chemical  
252 reaction, and the validity of the calculated ratio of cooling loss was assessed.

253 At the  $\theta_{pilot}$  of  $-34^\circ\text{CA}$  ATDC, the indicated thermal efficiency increases with the  
254 increase of the  $\text{O}_3$  concentration, and the excess of  $\text{O}_3$  decreases the indicated thermal  
255 efficiency. This is because with the increase of the  $\text{O}_3$  concentration, the degree of  
256 constant volume heat release,  $\eta_{glh}$ , and the combustion efficiency increase,  $\eta_{comb}$ , while  
257 the cooling loss,  $\varphi_{cool}$ , increases due to the advanced combustion phase. Further, the  
258 degree of constant volume heat release decreases with the excess amounts of the  $\text{O}_3$ ,  
259 higher than 170 ppm. At the  $\theta_{pilot}$  of  $-4^\circ\text{CA}$  ATDC, the indicated thermal efficiency  
260 increases with the increase in the  $\text{O}_3$  concentration, as the increase of the  $\text{O}_3$  concentration  
261 increases the degree of constant volume heat release and the combustion efficiency. With

262 the late pilot injection, the higher O<sub>3</sub> concentration is needed to improve the indicated  
263 thermal efficiency above that with the early pilot injection.

264 Figure 8 shows the indicated thermal efficiency,  $\eta_i$ , CA50, the THC and NO<sub>x</sub>  
265 emissions, and the O<sub>3</sub> concentration, at which the best indicated thermal efficiency can  
266 be achieved. The test results without the O<sub>3</sub> addition are shown for reference. The  
267 indicated thermal efficiency is improved with the O<sub>3</sub> addition for all the pilot injection  
268 timings. At the  $\theta_{pilot}$  of -30°CA ATDC, the indicated thermal efficiency without the O<sub>3</sub>  
269 addition becomes close to that with the O<sub>3</sub> addition. Without the O<sub>3</sub> addition, the degree  
270 of constant volume heat release decreases due to the retardation of the CA50, and the  
271 combustion efficiency decreases as seen in the increase of the unburned emissions, but  
272 the retardation of the CA50 decreases the cooling loss. This result suggests that there is  
273 an optimal CA50 at which the indicated thermal efficiency is increased.

274 The higher O<sub>3</sub> concentration is needed to achieve the best indicated thermal  
275 efficiency at the later pilot injection timings, while the best indicated thermal efficiency  
276 can be achieved at pilot injection timings earlier than -20°CA ATDC with lower O<sub>3</sub>  
277 concentrations. The O<sub>3</sub> addition reduces the THC emissions and increases the NO<sub>x</sub>  
278 emissions for all the pilot injection timings, but the lower NO<sub>x</sub> emissions can be achieved  
279 with the early pilot injection. Overall, the O<sub>3</sub> addition with the early pilot injection is

280 advantageous in terms of the lower O<sub>3</sub> concentration needed to achieve higher thermal  
281 efficiency, and low THC and NO<sub>x</sub> emissions.

282 **3.2. Variations in ozone concentration and pilot injection timing, and optimization**  
283 **of indicated thermal efficiency over a range of equivalence ratios of natural gas**

284 Operating conditions achieving the best thermal efficiency were investigated over a  
285 range of equivalence ratios of natural gas while varying the O<sub>3</sub> concentration and the pilot  
286 injection timing of diesel fuel.

287 The experimental conditions are detailed in Table 4. The equivalence ratio of natural  
288 gas,  $\phi_{\text{gas}}$ , was varied from 0.33 to 0.53 while the pilot injection quantity of the diesel fuel  
289 was fixed. Due to a failure of the injector used in section 3.1, a different injector equipped  
290 with a nozzle with nominal specifications identical to the nozzle used in section 3.1 was  
291 used. There were, however, differences in the injection quantity between the injectors. As  
292 a result, the pilot injection quantity of the diesel fuel was slightly larger in this experiment.  
293 No EGR and no supercharging were employed in the experiments to examine the effects  
294 of the equivalence ratio without any complexity.

295 As explained in section 3.1, a higher O<sub>3</sub> concentration is needed to enhance the  
296 combustion at the later pilot injection timings, while the combustion is enhanced with a



297 lower O<sub>3</sub> concentration at the early pilot injection timings. Considering this, the O<sub>3</sub>  
298 concentration was varied from 0 ppm to 280 ppm at the pilot injection timings from -  
299 69°CA ATDC to -29°CA ATDC, and from 0 ppm to 520 ppm at the pilot injection timings  
300 from -19°CA ATDC to 1°CA ATDC. The O<sub>3</sub> concentration was increased unless the  
301 indicated thermal efficiency begun to decrease with the increase of the O<sub>3</sub>. A larger flow  
302 rate of O<sub>2</sub> was needed to produce a higher concentration of O<sub>3</sub>, however it was difficult  
303 to control the O<sub>3</sub> concentration precisely with the larger flow rate of O<sub>2</sub>. To overcome this,  
304 the flow rate of the O<sub>2</sub> was changed with the pilot injection timings. As a result, the intake  
305 O<sub>2</sub> concentration was 20.6 vol.% at the pilot injection timings from -69°CA ATDC to -  
306 29°CA ATDC, and 21.5 vol.% at the pilot injection timings from -19°CA ATDC to 1°CA  
307 ATDC. The differences in the intake O<sub>2</sub> concentrations have a limited effect on engine  
308 performance and exhaust emissions, since it was confirmed that the experimental results  
309 for the various pilot injection timings show a similar tendency to that obtained in section  
310 3.1.

311 In the following experiments, first, the engine performance and the pilot injection  
312 timings encountering the occurrence of knocking and misfiring were examined without  
313 the O<sub>3</sub> addition. Figure 9 compares the indicated thermal efficiency,  $\eta_i$ , with the  
314 equivalence ratios of the natural gas,  $\phi_{\text{gas}}$ . The limit of the operations due to the misfiring

315 and knocking are superimposed. The operation with the  $\varphi_{\text{gas}}$  of 0.33 results in a low  
316 indicated thermal efficiency, and the late and early injections are limited by misfiring due  
317 to the combustion of the lean fuel-air mixture. With the higher  $\varphi_{\text{gas}}$  at 0.39 and 0.45, the  
318 indicated thermal efficiency increases primarily due to the improvement in the  
319 combustion efficiency, and the pilot injection without misfiring can be advanced. In  
320 analogy with the trend in Fig.8, the higher indicated thermal efficiency can be achieved  
321 at the earlier pilot injection timings with the  $\varphi_{\text{gas}}$  of 0.39 and 0.45. For the  $\varphi_{\text{gas}}$  of 0.53, the  
322 pilot injection timing is limited to the late crank angles due to knocking. The indicated  
323 thermal efficiency for the  $\varphi_{\text{gas}}$  of 0.53 is higher than the 0.39 and 0.45  $\varphi_{\text{gas}}$  at the late pilot  
324 injection timings of  $-4^{\circ}\text{CA ATDC}$  and  $1^{\circ}\text{CA ATDC}$ , while the highest thermal efficiency  
325 of the  $\varphi_{\text{gas}}$  of 0.39 and 0.45, which can be achieved at the earliest pilot injection timings,  
326 is almost equivalent to the thermal efficiency of the  $\varphi_{\text{gas}}$  of 0.53.

327       Second, the  $\text{O}_3$  was introduced, and the pilot injection timing was varied within the  
328 range where no knocking and misfiring occur. Figure 10 shows the effects of the  $\text{O}_3$   
329 concentration on the fuel mass burned at the 50% crank angle, CA50. With the pilot  
330 injection timing,  $\theta_{\text{pilot}}$ , later than  $-9^{\circ}\text{CA ATDC}$ , the  $\text{O}_3$  addition has a limited effect on the  
331 CA50 at all the equivalence ratios of the natural gas,  $\varphi_{\text{gas}}$ . For the  $\varphi_{\text{gas}}$  of 0.33 and 0.45,  
332 advances of the  $\theta_{\text{pilot}}$  from  $-29^{\circ}\text{CA ATDC}$  cause retardations of the CA50, and the CA50

333 is advanced with the increase of the O<sub>3</sub> concentration. In the present study, it was possible  
334 to operate the engine at the  $\theta_{\text{pilot}}$  of -69°CA ATDC with the aid of the O<sub>3</sub> for the  $\phi_{\text{gas}}$  at  
335 0.33, while it was not possible to establish conditions under which the  $\theta_{\text{pilot}}$  earlier than -  
336 49°CA ATDC could be set without causing misfiring and knocking for the  $\phi_{\text{gas}}$  of 0.45.  
337 Further, with the  $\theta_{\text{pilot}}$  earlier than -4°CA ATDC was limited by knocking with the  $\phi_{\text{gas}}$  of  
338 0.53.

339 Figure 11 shows the indicated thermal efficiency,  $\eta_i$ , the degree of constant volume  
340 heat release,  $\eta_{\text{glh}}$ , the combustion efficiency,  $\eta_{\text{comb}}$ , and the cooling loss,  $\phi_{\text{cool}}$ , for the  $\phi_{\text{gas}}$   
341 of 0.33. Without the O<sub>3</sub> addition, the lower indicated thermal efficiency is mainly due to  
342 the lower combustion efficiency that is caused by the combustion of the lean natural gas  
343 mixture. The O<sub>3</sub> addition improves the combustion efficiency and the degree of constant  
344 volume heat release noticeably with the  $\theta_{\text{pilot}}$  earlier than -49°CA ATDC due to the  
345 combustion promotion effect. The excess of O<sub>3</sub>, however, decreases the indicated thermal  
346 efficiency with the  $\theta_{\text{pilot}}$  at -49°CA ATDC since the CA50 is advanced, and the cooling  
347 loss is increased. With the  $\theta_{\text{pilot}}$  at -69°CA ATDC, a simultaneous higher combustion  
348 efficiency and lower cooling loss is obtained with the O<sub>3</sub> addition because the  $\theta_{\text{pilot}}$  of -  
349 69°CA ATDC allows the moderately late CA50 that reduces the cooling loss. As a result,  
350 the highest indicated thermal efficiency of 41.6% is attained at the  $\theta_{\text{pilot}}$  of -69°CA ATDC

351 with the 140 ppm O<sub>3</sub>. Figure 12 shows the indicated thermal efficiency,  $\eta_i$ , and the factors  
352 related to the thermal efficiency for the  $\phi_{\text{gas}}$  at 0.45. Unlike the  $\phi_{\text{gas}}$  at 0.33, the higher  
353 indicated thermal efficiency can be achieved at the  $\theta_{\text{pilot}}$  of -69°CA without the O<sub>3</sub> addition  
354 due to the better combustion efficiency. With an increase of the O<sub>3</sub> concentration to  
355 around 50 ppm, the indicated thermal efficiency increases due to the improvements in the  
356 combustion efficiency and the degree of constant volume heat release increase while  
357 maintaining the lower cooling loss. The further increase of the O<sub>3</sub> concentration, however,  
358 increases the cooling loss. As a result, the highest indicated thermal efficiency of 41.7%  
359 is attained at the  $\theta_{\text{pilot}}$  of -49°CA ATDC with the 30 ppm O<sub>3</sub>. Figure 13 shows the indicated  
360 thermal efficiency,  $\eta_i$ , and the factors related to the thermal efficiency for the  $\phi_{\text{gas}}$  at 0.53.  
361 The pilot injection timings are limited to -4°CA ATDC and 1°CA ATDC. At the late pilot  
362 injection timings, the O<sub>3</sub> addition slightly increases the degree of constant volume heat  
363 release and the cooling loss due to the advanced CA50, and the O<sub>3</sub> addition has a limited  
364 effect on the indicated thermal efficiency.

365 Figure 14 shows the effect of the O<sub>3</sub> concentration on the maximum rate of pressure  
366 rise,  $(dp/d\theta)_{\text{max}}$ , over the range of equivalence ratios of the natural gas,  $\phi_{\text{gas}}$ . The increase  
367 in the  $(dp/d\theta)_{\text{max}}$  with the O<sub>3</sub> addition is more remarkable for the pilot injection timings,  
368  $\theta_{\text{pilot}}$ , earlier than -29°CA ATDC for (a) the  $\phi_{\text{gas}}$  of 0.33 and (b) the  $\phi_{\text{gas}}$  of 0.45. This is

369 because the O<sub>3</sub> addition advances the combustion phase of the single-stage combustion at  
370 the early pilot injection, while the O<sub>3</sub> addition with the late pilot injection has a limited  
371 effect on the first stage combustion which determines the maximum rate of pressure rise,  
372 as can be seen in Fig.5. For (c) the  $\varphi_{\text{gas}}$  of 0.53, the  $(dp/d\theta)_{\text{max}}$  increases with the increase  
373 of the O<sub>3</sub> concentration at the late pilot injection of the  $\theta_{\text{pilot}}$  of -9°CA ATDC as the ROHR  
374 at second stage combustion becomes large and increases the maximum rate of pressure  
375 rise.

376 The early pilot injections with the O<sub>3</sub> addition lead to the lower  $(dp/d\theta)_{\text{max}}$  compared  
377 to the  $\theta_{\text{pilot}}$  of -9°CA ATDC for (a) the  $\varphi_{\text{gas}}$  of 0.33, and for (b) the  $\varphi_{\text{gas}}$  of 0.45, the early  
378 pilot injections with the O<sub>3</sub> addition cause too much advanced CA50 as seen in Fig.10  
379 and lead to the higher  $(dp/d\theta)_{\text{max}}$ . This result suggests that the combination of the early  
380 pilot injection and the O<sub>3</sub> addition can be used with an acceptable level of the maximum  
381 rate of pressure rise at lower equivalence ratio of the natural gas while achieving an  
382 optimal CA50.

383 Figure 15 shows the indicated thermal efficiency,  $\eta_i$ , the THC and NO<sub>x</sub> emissions,  
384 the pilot injection timing,  $\theta_{\text{pilot}}$ , and the O<sub>3</sub> concentration, at which the best indicated  
385 thermal efficiency can be achieved. The test results without the O<sub>3</sub> addition are shown for  
386 reference. The improvements in the indicated thermal efficiency and the THC emissions

387 with the O<sub>3</sub> addition are most remarkable for the equivalence ratio of natural gas,  $\phi_{\text{gas}}$ , of  
388 0.33, where the  $\theta_{\text{pilot}}$  is advanced to -69°CA ATDC, and the O<sub>3</sub> concentration is at 140  
389 ppm. Without the aid of the O<sub>3</sub>, it is difficult to implement the early pilot injection due to  
390 misfiring. With the increase of the  $\phi_{\text{gas}}$ , the best pilot injection timing is retarded, the best  
391 O<sub>3</sub> concentration decreases, and the differences with and without the O<sub>3</sub> addition become  
392 small. For the  $\phi_{\text{gas}}$  0.53, the best indicated thermal efficiency is obtained without the O<sub>3</sub>  
393 addition at the  $\theta_{\text{pilot}}$  near top dead center. There are no remarkable differences in the NO<sub>x</sub>  
394 emissions with and without the O<sub>3</sub> addition over a range of  $\phi_{\text{gas}}$ .

#### 395 **4. Conclusions**

396 To improve the thermal efficiency and exhaust emissions of natural gas fueled engines  
397 ignited by diesel fuel (natural gas – diesel dual fuel engines) with the ignition  
398 enhancement effects of O<sub>3</sub>, an experimental study was carried out in a single cylinder  
399 engine while varying the O<sub>3</sub> concentration at the intake port and the pilot injection timing  
400 of the diesel fuel. Further, the equivalence ratio of the natural gas was varied from 0.33  
401 to 0.53 to elucidate the changes in the requirement for the O<sub>3</sub> concentration. The  
402 conclusions may be summarized as follows:

403 1. In the natural gas – diesel dual fuel engines, a two-stage heat release takes place with

404 the late pilot injection. The first stage is a heat release by the mixture of the diesel fuel  
405 and the natural gas, and the O<sub>3</sub> addition has little influence on the rate of heat release.  
406 The second stage is a heat release by the natural gas which is not mixed well with the  
407 diesel fuel, and O<sub>3</sub> of the order of several hundred ppm is needed to increase the rate  
408 of heat release. With the early pilot injection, a single-stage heat release takes place,  
409 and the ignition timing and the combustion phase are advanced with the O<sub>3</sub>  
410 concentration lower than 100 ppm.

411 2. With the O<sub>3</sub> addition, the unburned hydrocarbons decrease, the NO<sub>x</sub> emissions  
412 increase, and the early injection timing can be advanced without misfiring.

413 3. The O<sub>3</sub> concentration needed to achieve the best indicated thermal efficiency can be  
414 reduced more with the early pilot injection, compared to the late pilot injection. In  
415 addition, the lower unburned hydrocarbons and NO<sub>x</sub> emissions can be achieved with  
416 the combination of the O<sub>3</sub> addition and the early pilot injection.

417 4. The O<sub>3</sub> addition increases the maximum rate of pressure rise notably for the early pilot  
418 injection. The operation with an acceptable level of the maximum rate of pressure rise,  
419 however, can be achieved at lower equivalence ratio of the natural gas while achieving  
420 optimal combustion phase.

421 5. The improvement in the indicated thermal efficiency and the reduction of the

422 unburned hydrocarbons with the O<sub>3</sub> addition are more pronounced for lower  
423 equivalence ratios of the natural gas, while the O<sub>3</sub> addition has a limited effect on the  
424 indicated thermal efficiency and the unburned hydrocarbons for higher equivalence  
425 ratio of the natural gas. This would suggest that the combination of the O<sub>3</sub> addition  
426 and supercharging which reduces the equivalence ratio and decreases the cooling loss  
427 is a means to improve the thermal efficiency and emissions at higher engine loads.  
428 Further, the use of EGR along with the O<sub>3</sub> addition may improve the indicated thermal  
429 efficiency due to the decrease in the cooling loss while avoiding misfiring caused by  
430 the dilution of mixtures.

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## 515 APPENDIX

516 Here, the electric energy consumption needed to produce the ozone (O<sub>3</sub>) is calculated.  
 517 The ozonizer used in the present study (EcoDesign, ED-OG-S4AD) is not manufactured  
 518 specifically for the use in internal combustion engines, and its energy consumption may  
 519 not be suitable for the evaluation. Instead, data of an intake in-line type ozonizer  
 520 manufactured for gasoline engines, which can be found in Ref.[19], were employed to  
 521 determine the energy consumption.

522 According to Ref.[19], the electric energy consumption of 60 W is needed to produce  
 523 the O<sub>3</sub> concentration, [O<sub>3</sub>], of 50 ppm with the flow rate of air at 0.2 m<sup>3</sup>/min with the  
 524 intake in-line type ozonizer using dielectric-barrier discharge. For simplicity, the present  
 525 calculation assumed that the electric energy consumption is proportional to the produced  
 526 O<sub>3</sub> concentration and to the flow rate of air. Further, assuming that the volumetric  
 527 efficiency of the engine is unity, the electric energy consumption,  $E$  [W], needed to  
 528 produce [O<sub>3</sub>] [ppm] is expressed as follows:

$$529 \quad E \text{ [W]} = 60 \text{ [W]} \times \frac{V_h \cdot n \cdot i \text{ [m}^3/\text{s}]}{0.2 \text{ [m}^3/\text{s}]} \times \frac{[\text{O}_3] \text{ [ppm]}}{50 \text{ [ppm]}} \quad (\text{A1})$$

530 Here,  $V_h$  is the stroke volume [m<sup>3</sup>],  $n$  is the engine rotation speed [rpm], and  $i$  is 1/2  
 531 for four stroke-cycle engines.

532 The power output,  $N_p$ , [W] is expressed with the following relation:

$$533 \quad N_p \text{ [W]} = p_{me} \text{ [Pa]} \cdot \left( V_h \cdot \frac{n}{60} \cdot i \right) \text{ [m}^3/\text{s}] \quad (\text{A2})$$

534 Here,  $p_{me}$  is the mean effective pressure [Pa].

535 The ratio of the energy consumption due to the O<sub>3</sub> production,  $\gamma$ , is defined as follows:

$$536 \quad \gamma \text{ [%]} = \frac{E}{N_p} \times 100 = \frac{3600}{0.2 \times 50} \frac{[\text{O}_3]}{p_{me}} \times 100 \quad (\text{A3})$$

537 The calculated ratio of the energy consumption,  $\gamma$ , versus the mean effective pressure,  
 538  $p_{me}$ , with the variation of the O<sub>3</sub> concentration is shown in Fig.A-1. The ratio of the energy

539 consumption,  $\gamma$ , increases with the increase of the O<sub>3</sub> concentration, and the energy  
540 consumption is significant at the lower brake mean effective pressure.